

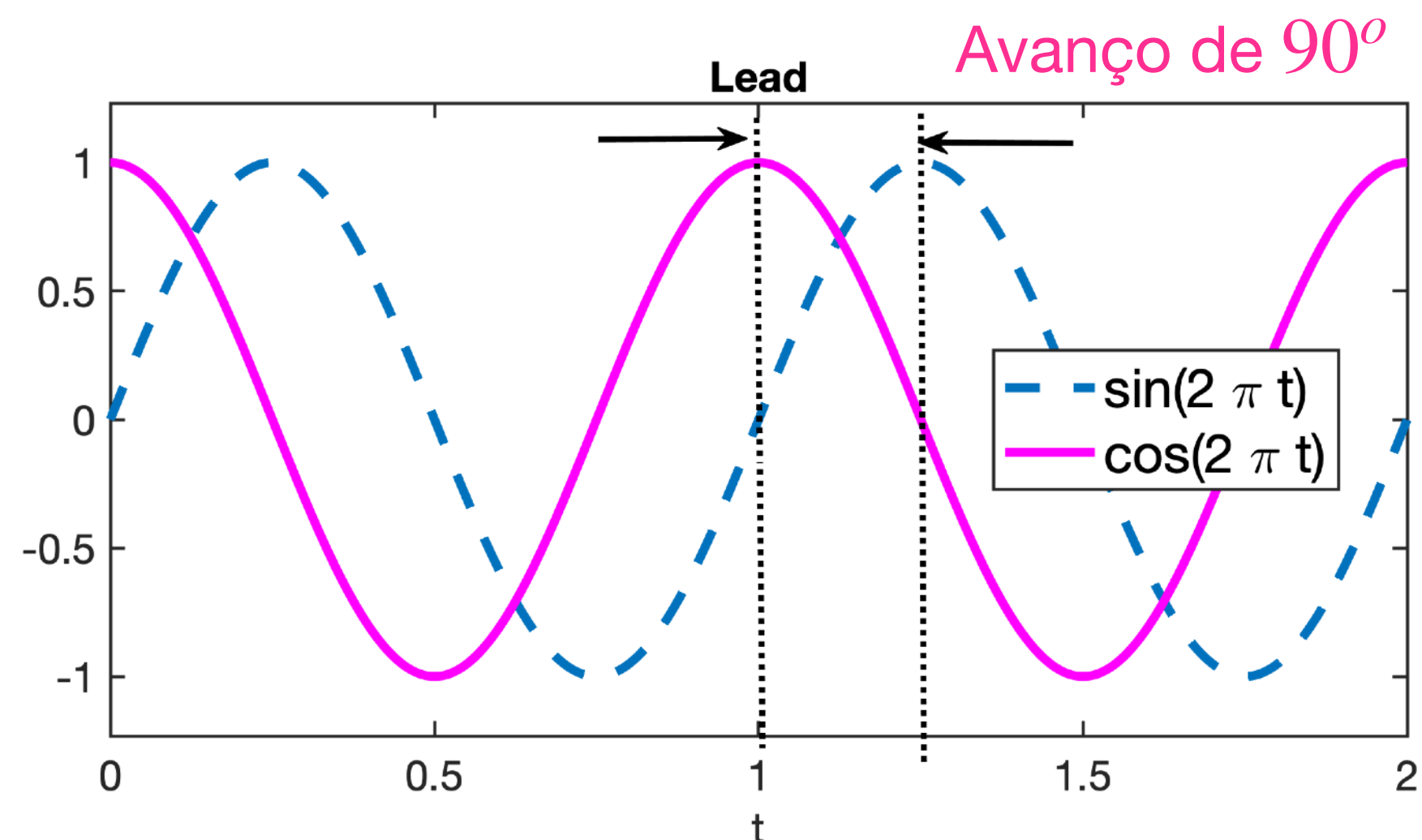
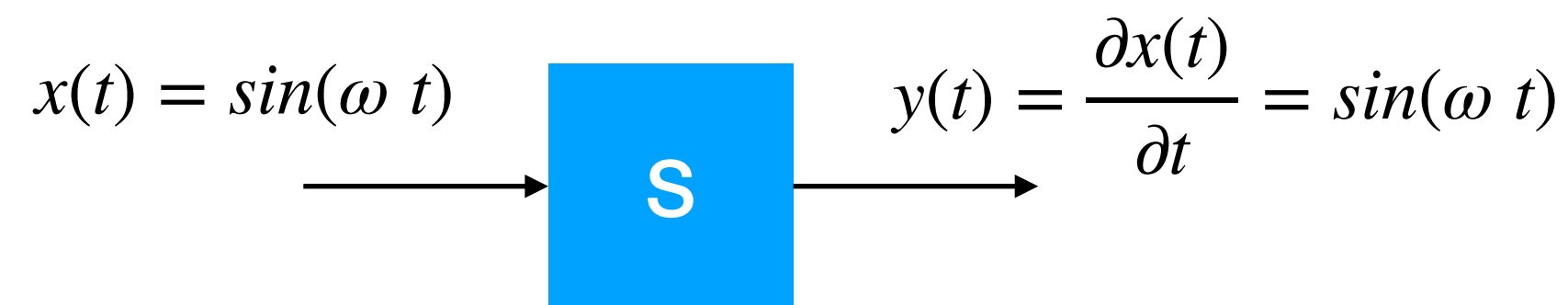
# Controladores Lead/Lag

Técnicas de Resposta em Frequência  
Prof. Fernando Passold

# Controlador Lead (Avanço de Fase)

- Fatos:

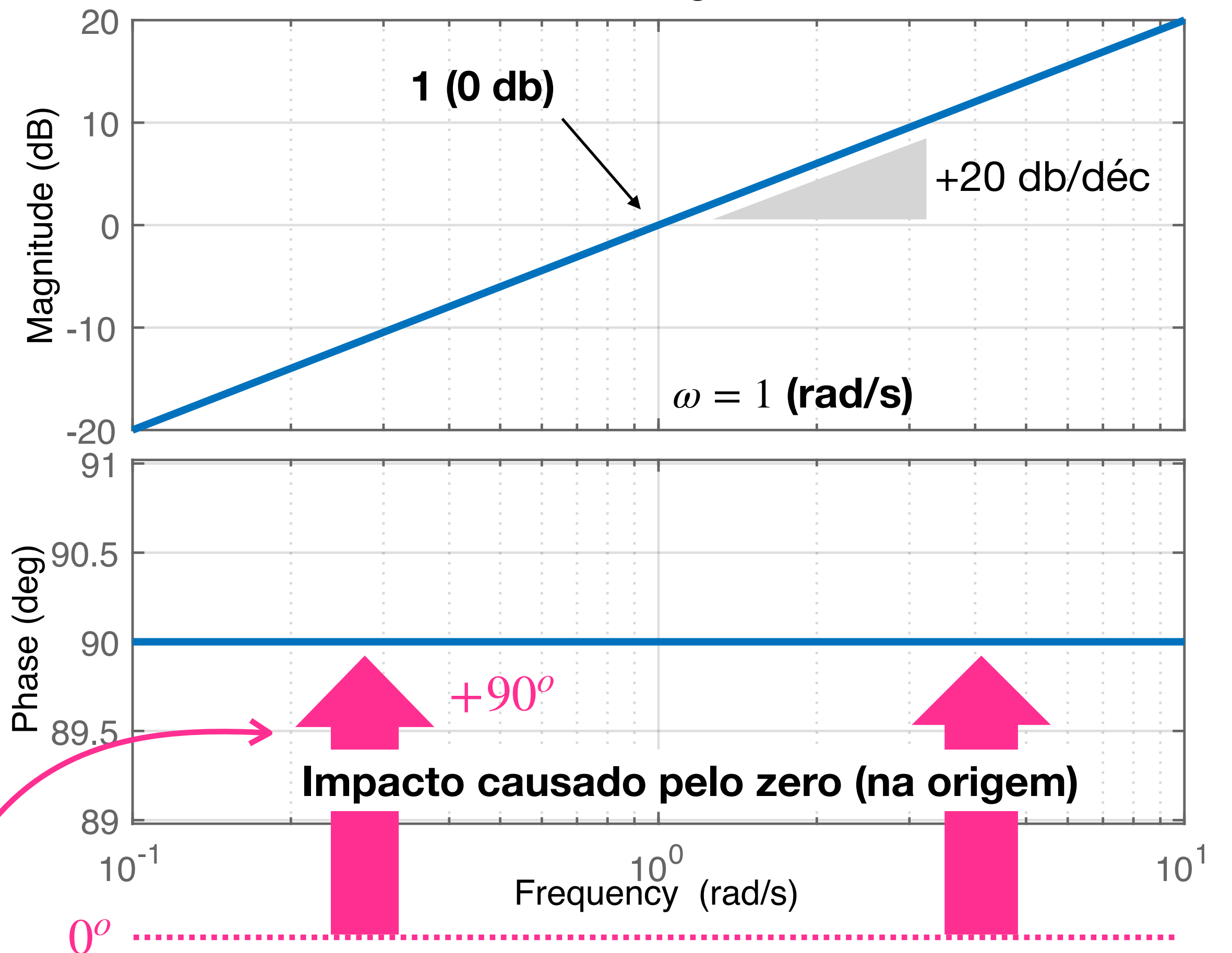
Derivativo Puro:  $C(s) = K \cdot s$



```
>> figure; ezplot('sin(2*pi*t)', [0 2])
>> hold on; ezplot('cos(2*pi*t)', [0 2])
>> title('Lead')
>> legend('sin(2 \pi t)', 'cos(2 \pi t)')
```

“Soma fase”

Bode Diagram



# Controlador Lead (Avanço de Fase)

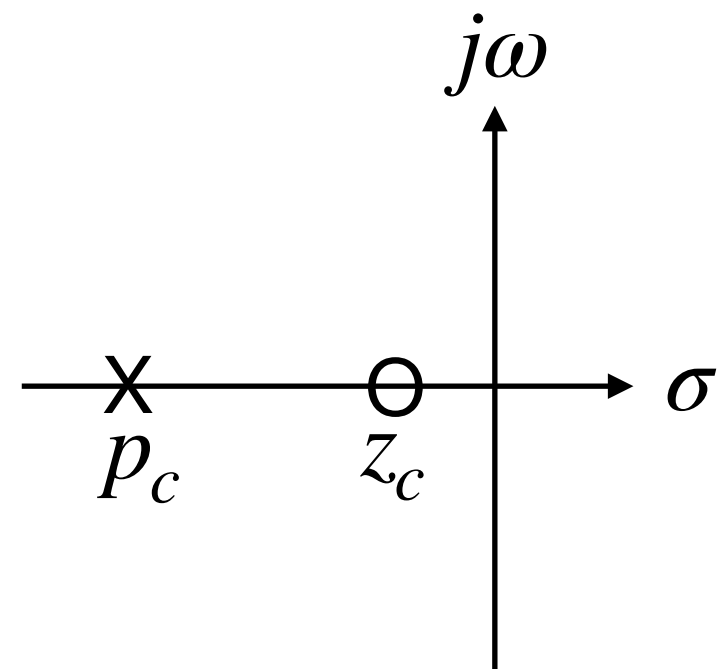
- Base teórica:

$$\text{Controlador: } C(s) = \underbrace{\left( \frac{\omega_p}{\omega_z} \right)}_K \cdot \frac{(s + \omega_z)}{(s + \omega_p)}$$

Zero  $\Rightarrow$  próximo da origem (do plano-s)

$$\text{e } \omega_z < \omega_p$$

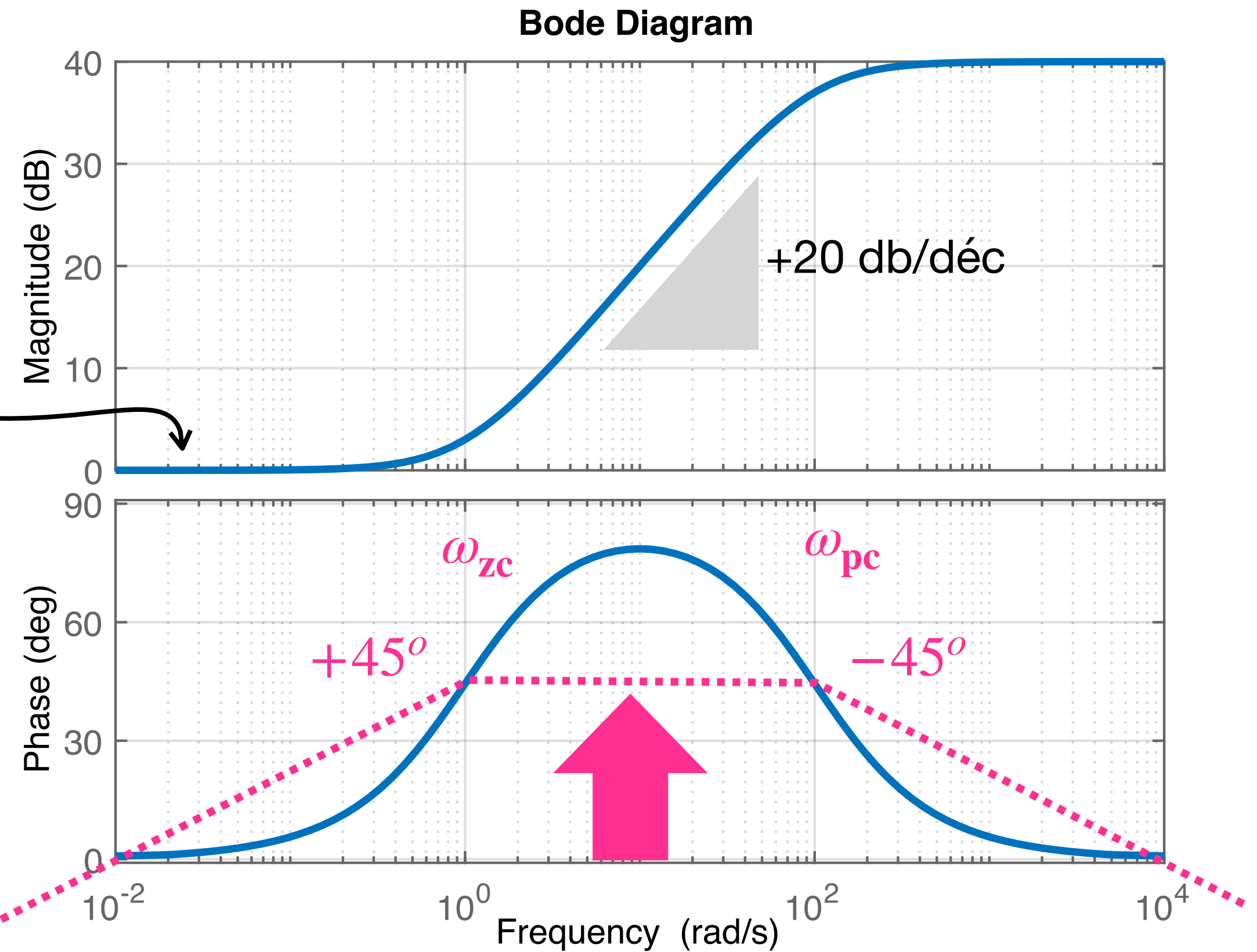
1 (0 db)



```
>> G_lead=tf(100*[1 1],[1 100]);
>> zpk(G_lead)
ans =
```

$$\frac{100 (s+1)}{(s+100)}$$

```
Continuous-time zero/pole/gain model.
>> figure; bode(G_lead)
```

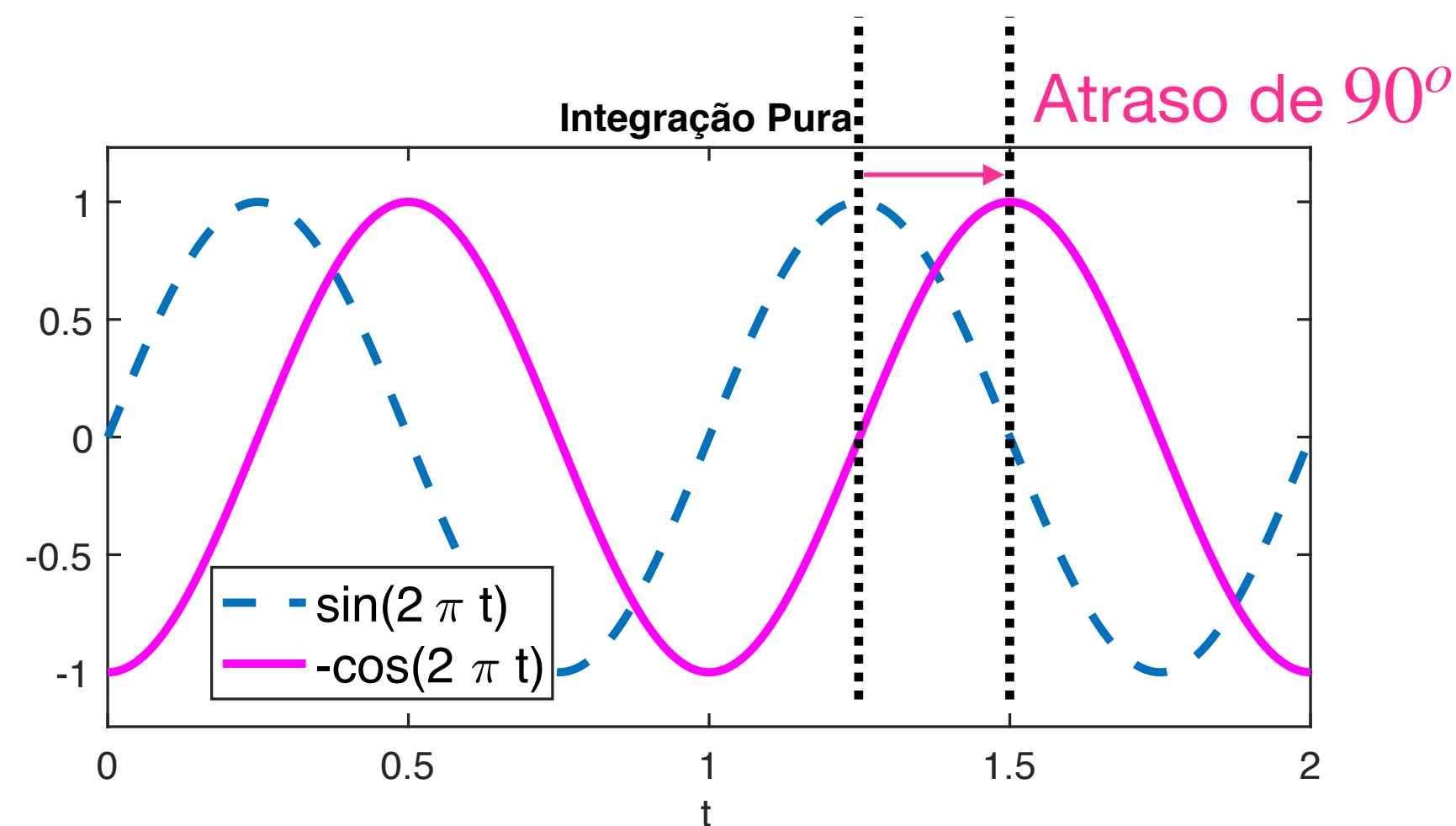
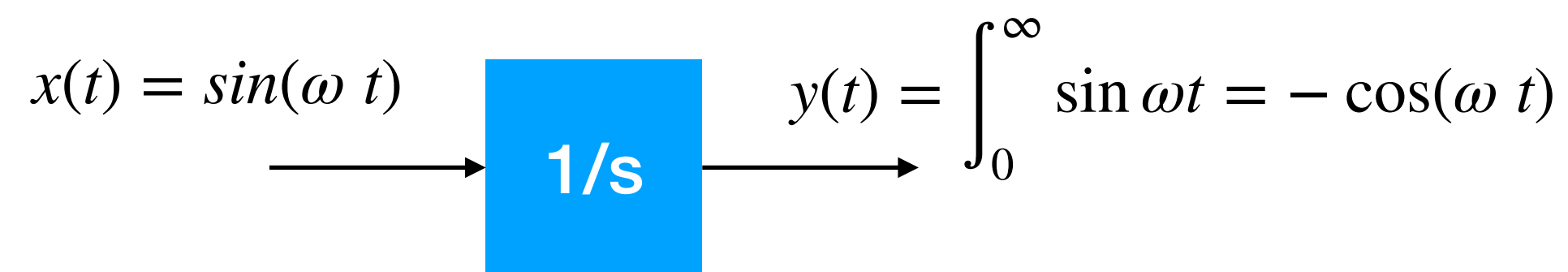


- Vantagens:**
- aumenta margem de fase,  $\Phi_m \Rightarrow \propto \% OS, \zeta \downarrow$  ;
  - $\downarrow t_r, \downarrow t_s$
  - **Faixa alta de frequências...**

# Controlador Lag (Atraso de Fase)

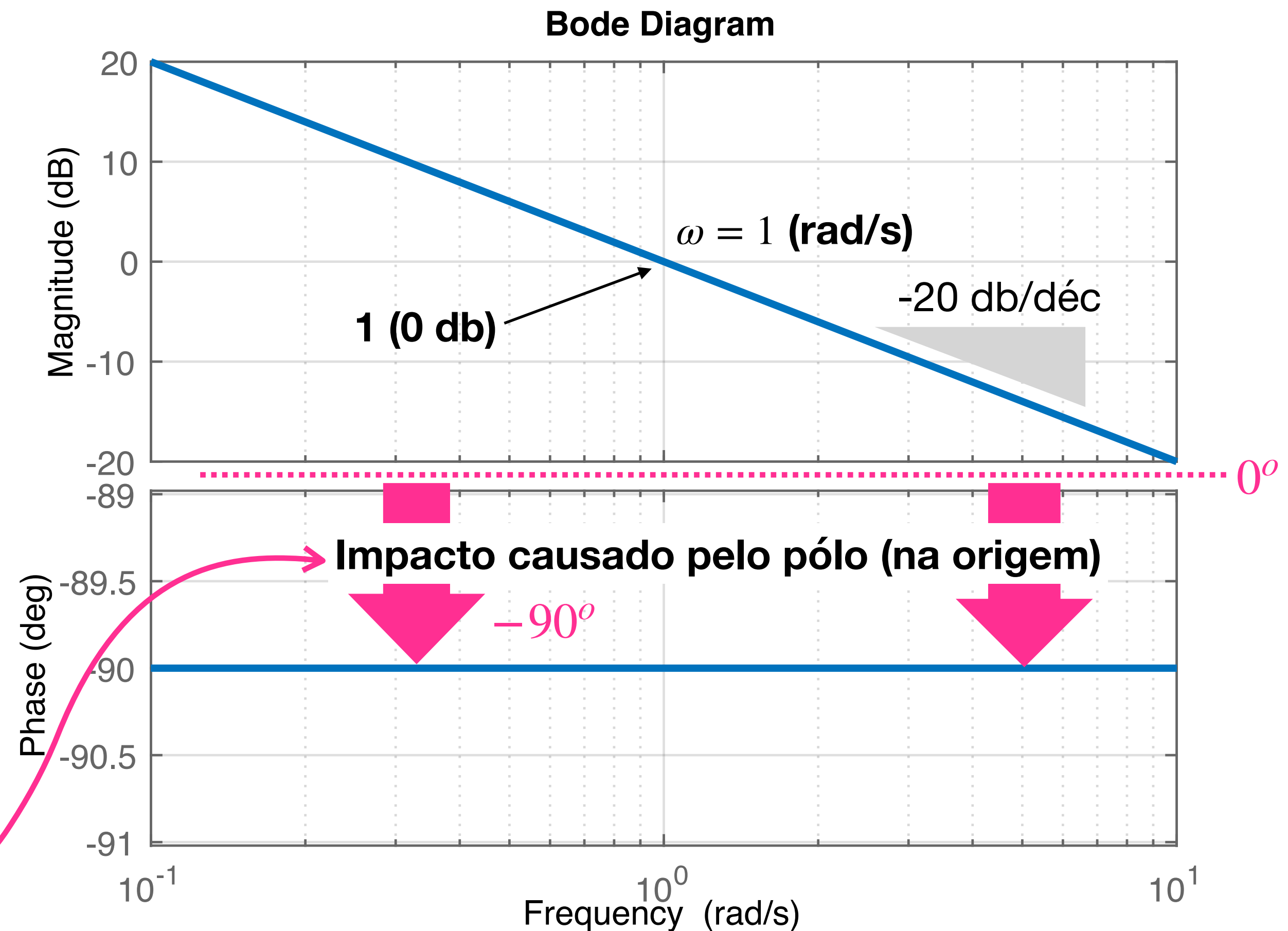
- Fatos:

Integrador Puro:  $C(s) = K \cdot \frac{1}{s}$



```
>> figure; ezplot('sin(2*pi*t)', [0 2])
>> hold on; ezplot('-cos(2*pi*t)', [0 2])
>> title('Integração Pura');
>> legend('sin(2 \pi t)', '-cos(2 \pi t)')
```

“Atrasa fase”



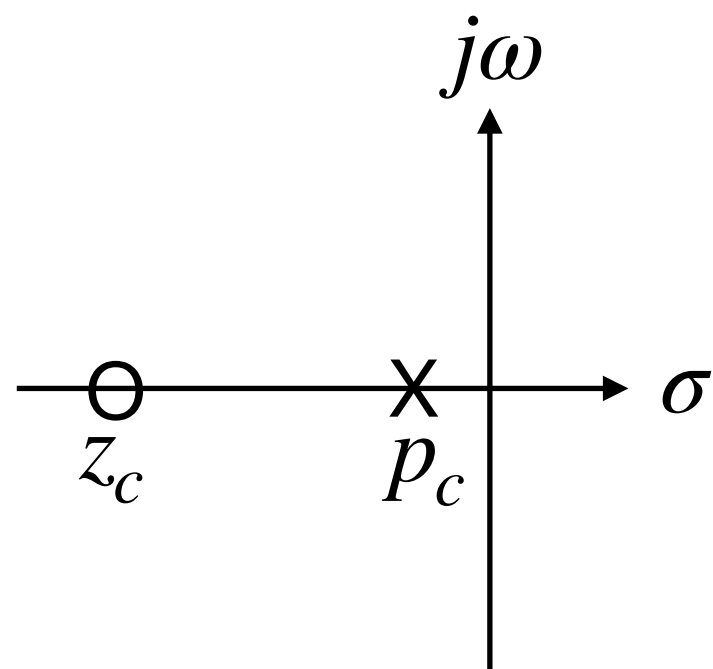
# Controlador Lag (Atraso de Fase)

- Base teórica:

$$\text{Controlador: } C(s) = \underbrace{\left( \frac{\omega_p}{\omega_z} \right)}_K \cdot \frac{(s + \omega_z)}{(s + \omega_p)}$$

Pólo  $\Rightarrow$  próximo da origem (do plano-s)

e  $\omega_p < \omega_z$



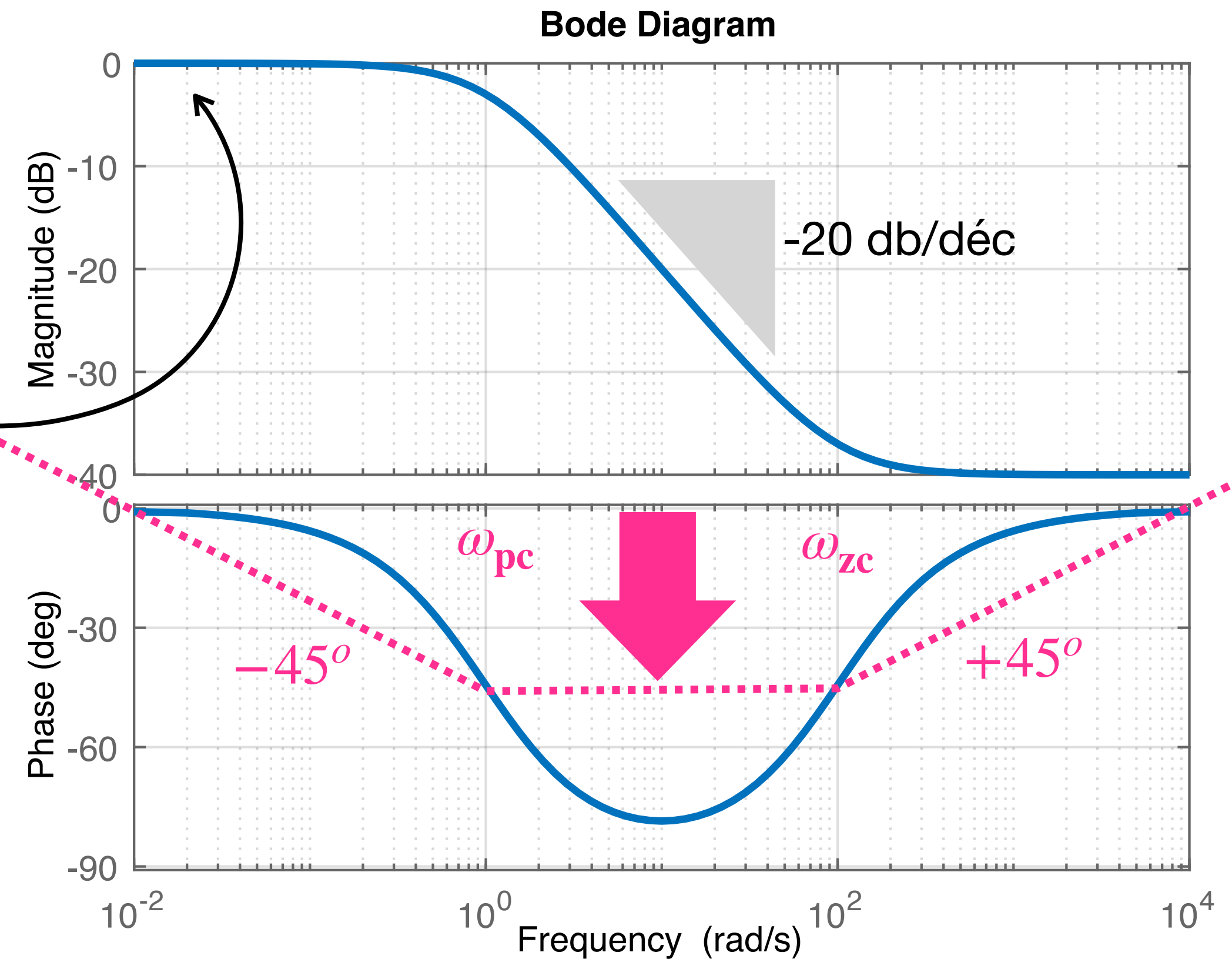
```
>> G_lag=tf((1/100)*[1 100],[1 1]);
>> zpk(G_lag)

ans =

    0.01 (s+100)
    -----
           (s+1)

Continuous-time zero/pole/gain model.

>> figure; bode(G_lag)
```

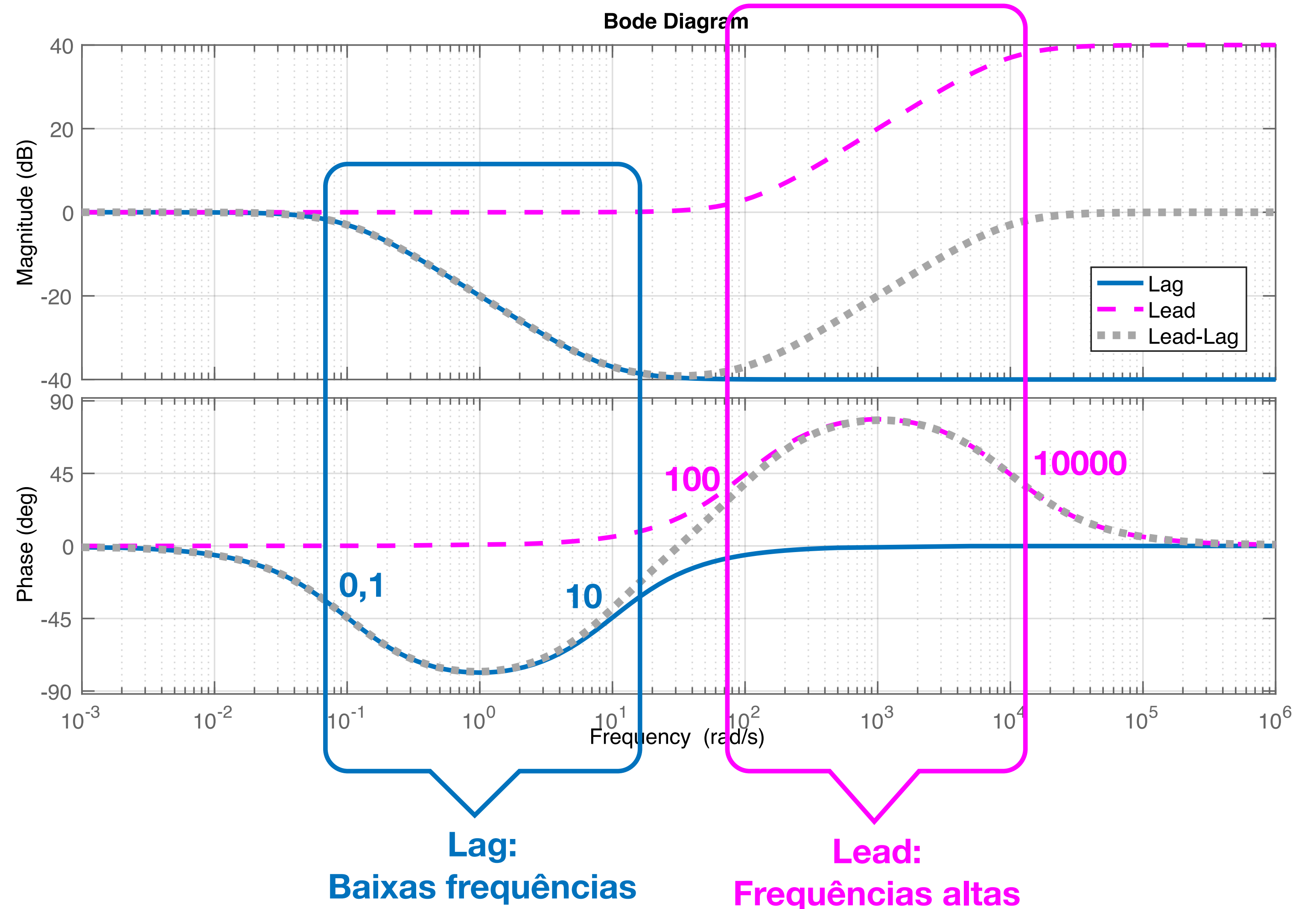


- Vantagens:**
- Melhora resposta do Lead:  $e(\infty) \downarrow$  ;
  - Mas diminui margem de fase,  $\Phi_M \downarrow$  ;
  - a relação:  $\frac{\text{zero}}{\text{pólo}} \propto K_p, K_v, K_a$  ;
  - Faixa baixa de frequências...

# Controlador Lead-Lag

- Efeito

```
>> G_lag=tf((0.1/10)*[1 10],[1 0.1]);  
>> zpk(G_lag)  
  
0.01 (s+10)  
-----  
(s+0.1)  
  
>> G_lead=tf((10000/100)*[1 100],[1 10000])  
>> zpk(G_lead)  
  
100 (s+100)  
-----  
(s+1e04)  
  
>> C=G_lag*G_lead;  
>> figure; bode(G_lag, G_lead, C)  
>> legend('Lag', 'Lead', 'Lead-Lag')  
>> grid
```



# Controlador Lag (Atraso de Fase)

- Efeito:

Objetivos:

1. Reduzir  $e(\infty) \downarrow$
2. Aumentar  $\Phi_M \uparrow \Rightarrow$  adequar  $\% OS, t_s, \zeta$

Passos:

- 1) Aumentar  $K$ ;
- 2) Encontrar  $\Phi_M$  (ou  $P_M$ )
- 3) Ajustar  $p_C$  e  $z_C$  para alcançar  $\Phi_m$  desejado
- 4) Voltar a ajustar  $K$  para compensar alguma queda (variação) trazida pelo compensador.

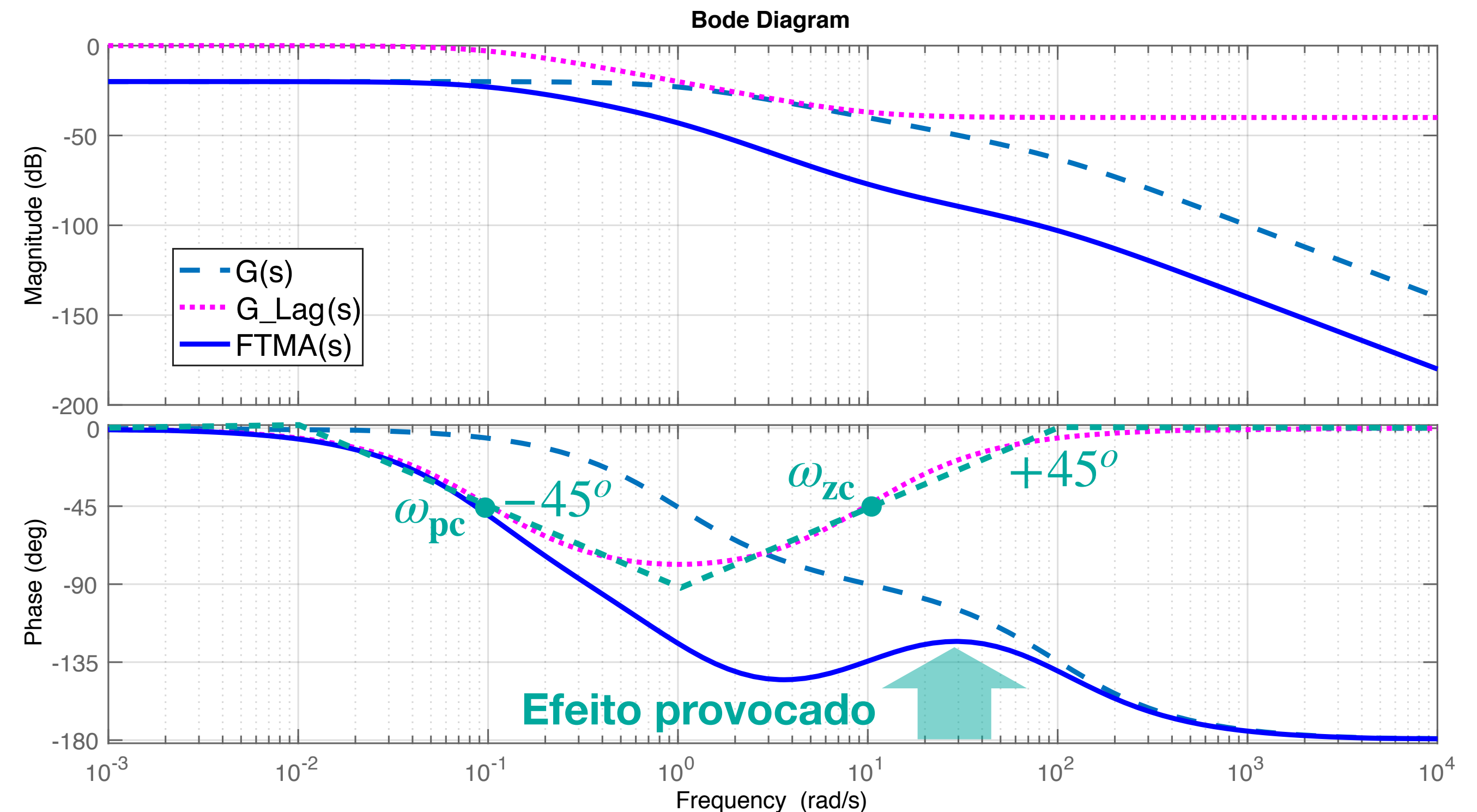
```
>> G=tf(10,poly([-1 -100]));
>> G_lag=tf((0.1/10)*[1 10],[1 0.1]);
>> ftma=G_lag*G;
>> figure; bode(G, G_lag, ftma)
>> zpk(G)

    10
-----
(s+100) (s+1)

>> zpk(G_lag)

    0.01 (s+10)
-----
    (s+0.1)

>>
```



Região de interesse:

Reduz fase da planta, aumentando margem de fase,  $\Phi_M$